



MATHEMATICS

9794/03

Paper 3 Applications of Mathematics

May/June 2019

MARK SCHEME

Maximum Mark: 80

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

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Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Question	Answer	Marks	Guidance
1(a)(i)	0.3	B1	AEF
1(a)(ii)	0.1	B1	AEF
1(a)(iii)	$\frac{3}{7}$	B1	Allow 0.429
1(b)	$P(B). P(T) = \frac{11}{30} \cdot \frac{7}{30}$ [$= \frac{77}{900} = 0.0855(5555555\dots)$]	M1	or $P(B) = \frac{11}{30}$
	(Compare with answer to 1(a)(ii) and) state NOT independent	A1	compare $P(B)$ with $P(B T)$
2(a)	Standardise 55 as $\frac{55-50}{15}$	M1	
	Use tables to get 0.63(0)	A1	Accept 0.631 Awr 0.630 or 0.631
2(b)	$P(X \leq 60) - P(X \leq 30)$	M1	
	$P(Z \leq 0.667) - P(Z \leq -1.333) = 0.7477 - (1 - 0.9087)$	M1	
	0.656	A1	Awr 0.656
2(c)	1.645	B1	
	$\frac{t-50}{15} = 1.645$	M1	Using <i>their</i> 1.645
	$t = 74.7$	A1	Awr to 74.7
3(a)	Attempt to find b using S_{xy}/S_{xx}	M1	E.g. 2.911/8.98
	Clearly get 0.324	A1	0.324164811
	Clearly get $a = 1.886 - 0.324164811 \times 4.2 = 0.525$	B1	
	Draw correct line on scatter graph	B1	
3(b)	Residuals shown	B1ft	FT <i>their</i> line
3(c)	State 0	B1	
3(d)	Attempt residuals and square	M1	
	Get 0.0812	A1	0.081211709 from a exact 0.081225138 from a as 0.324

Question	Answer	Marks	Guidance
4(a)	The probability of John connecting with a customer adviser is constant	B1	Must be in context
	Independence of connecting on successive attempts Unlimited number of calls possible within a day	B1	
4(b)(i)	$0.6^2 \times 0.4$	M1	
	$\frac{18}{125}$ or 0.144	A1	
4(b)(ii)	0.6^3 or $1 - (0.4 + 0.6 \times 0.4 + 0.6^2 \times 0.4)$	M1	
	$\frac{27}{125}$ or 0.216	A1	
4(c)	B(6, 0.216)	B1ft	FT their 0.216, may be implied
	${}^6C_2 \times 0.216^2 \times (1 - 0.216)^4$	M1	Using their binomial distribution with $n = 6$
	0.264	A1	
5(a)	12! or 479 001 600	B1	
5(b)	7! or 5! seen	B1	
	$2 \times 7! \times 5! = 1\,209\,600$	B1	
5(c)	Consider arrangement to get 8!	B1	
	Total number of arrangements of statistics books is 5!	B1	
	Get $\frac{8! \times 5!}{\text{their } 12!}$	M1	$8! \times 5! = 4\,838\,400$
	Get $\frac{1}{99}$	A1	0.0101

Question	Answer	Marks	Guidance
5(d)	Get $6! \times 4!$	B1	
	Separated by 9 or 10 books and a reasonable attempt at probability	M1	$\frac{k \times 6! \times 4!}{7! \times 5!} = \frac{3}{35}, k > 1$
	$\frac{3 \times 6! \times 4!}{7! \times 5!} = \frac{3}{35}$	A1	0.0857(14285)
	OR		
	Consider A in 1st position and 2nd position	B1	
	Attempt at $\frac{1}{7} \times \frac{2}{5} + \frac{1}{7} \times \frac{1}{5}$	M1	
	Get $\frac{3}{35}$	A1	0.0857(14285)
6(a)	Use $v = u + at = 4 \times 3 = 12$	B1	
6(b)	Use area under graph is distance	M1	
	$\frac{1}{2} \times 12 \times (30 + 40)$	A1ft	FT their v
	420m	A1ft	$35 \times v$
7(a)	Use of N2L on whole system with 5 terms	M1	Dimensionally correct, allow sign errors
	$2600 - 400 - 500 = 2700a$	A1	
	$a = 0.63(0) \text{ ms}^{-2}$	A1	Awrt 0.630
	OR		
	Use N2L on car (4 terms) OR caravan (3 terms)	M1	Dimensionally correct, allow sign errors
	$2600 - 500 - T = 1900a$ AND $T - 400 = 800a$	A1	
	Solve to get $a = 0.63(0) \text{ ms}^{-2}$	A1	Awrt 0.630

Question	Answer	Marks	Guidance
7(b)	Use N2L with their a on car (4 terms) OR caravan (3 terms)	M1	Dimensionally correct, allow sign errors
	$2600 - 500 - T = 1900a$ OR $T - 400 = 800a$	A1	<i>Their a</i> substituted
	$T = 904 \text{ N}$	A1	Awrt 904
	OR Use N2L on car (4 terms) OR caravan (3 terms)	M1	Dimensionally correct, allow sign errors
	$2600 - 500 - T = 1900a$ AND $T - 400 = 800a$	A1	
	Solve to get $T = 904 \text{ N}$	A1	Awrt 904
8(a)	$x = 44\cos 7 t$	B1	$x = 43.67203067t$; allow if x not the subject
	$y = 44\sin 7 t - \frac{1}{2} \cdot 10 \cdot t^2$	B1	$y = 5.36225111t - \frac{1}{2} \cdot 10 \cdot t^2$
	Eliminate t	M1	
	Get $y = 0.123x - 0.00262x^2$	A1	
8(b)	Substitute $x = 12$ in trajectory equation	M1	Or find t ($= 0.27477\dots$) from horizontal motion using a component of 44 and use in $s = ut + \frac{1}{2}at^2$ with $u =$ component of 44 and $a = -g$
	Get height $= 1.09872 + 2.6 = 3.7(0)$	A1	
	Substitute $y = -2.6$ into trajectory equation	M1	Or use $s = ut + \frac{1}{2}at^2$ with $s = -2.6$, $u =$ component of 44 and $a = -g$
	Attempt to solve 3 term quadratic equation	M1	Or solve 3 term quadratic for t ($= 1.4348\dots$) and use $x =$ (component of 44) t
	Get 50.7 only	A1	Allow 50.8; discard the other solution

Question	Answer	Marks	Guidance
9(a)	$R = 5g\cos 16$	B1	
	Use $F = 0.4 \times R$	M1	19.22523392; $R \neq 5g$
	Use N2L parallel to slope with 3 terms	M1	Dimensionally correct, allow sign errors
	$-5g\sin 16 - F = 5a$	A1	Allow $5g\sin 16 + F = 5a$; F need not be substituted, allow <i>their</i> F
	$a = \pm 6.6(01420342)$	A1	Allow $a = \pm \frac{(5g \sin 16 + 0.4 \times 5g \cos 16)}{5}$
	use $v = u + at$ with $v = 0$ and their a	M1	a must be -ve
	$t = 0.757s$	A1	Awrt 0.757
9(b)(i)	Compare weight component ($5g\sin 16$) down slope with F_{\max} ($2g\cos 16$)	M1	May be implied
	Get required friction to be $5g\sin 16 = 13.8$	A1	13.78186779
9(b)(ii)	50N, vertically upwards or 74° to slope and above	B1	oe
	Balances the weight	B1	
10(a)	$2v_A = 2 \times 5 - 6$ or $3v_B = 3 \times 1.5 + 6$	M1	Attempt at momentum-impulse equation
	$v_A = 2$	A1	
	$v_B = 3.5$	A1	
10(b)	Use conservation of momentum	M1	Allow sign errors
	$3 \times 3.5 = 3b + mc$	A1	FT <i>their</i> 3.5
	Use NEL	M1	Allow sign errors
	$b - c = -0.4 \times 3.5$	A1	FT Momentum and NEL must be consistent for both A1s
	Eliminate c to get an equation in b and m	M1	Dep on first two M1 $b = (10.5 - 1.4m)/(m+3)$
	Set $b \geq 2$	M1	Allow $>$ or $=$, FT their 2
	Get $m \leq 1.32$	A1	Allow 45/34